



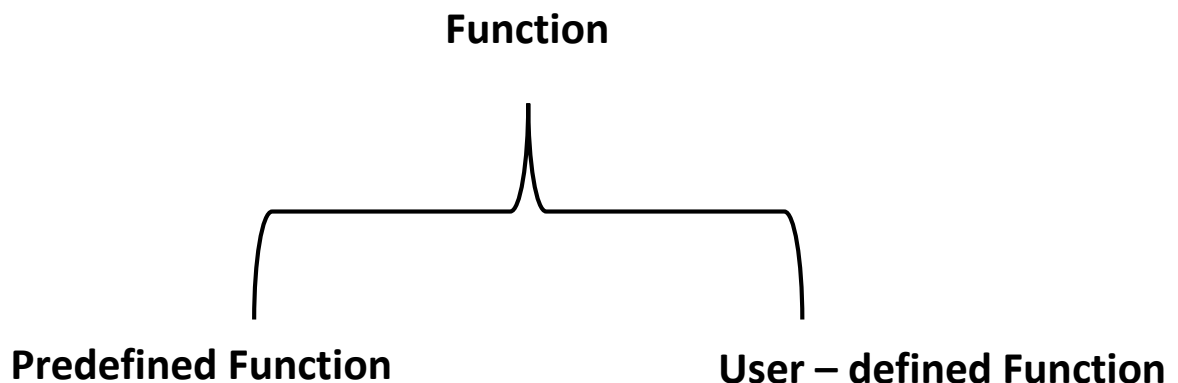
In this lecture you will learn:

- **Function**

Functions are like building blocks. They let you divide complicated programs into manageable pieces. They have other advantages, too:

- While working on one function, you can focus on just that part of the program and construct it, debug it, and perfect it.
- Different people can work on different functions simultaneously.
- If a function is needed in more than one place in a program or in different programs, you can write it once and use it many times.
- Using functions greatly enhances the program's readability because it reduces the complexity of the function main.

There is two type of function:



Predefined Functions

Function	Header File	Purpose	Parameter(s) Type	Result
<code>abs (x)</code>	<code><cmath></code>	Returns the absolute value of its argument: <code>abs (-7) = 7</code>	<code>int</code> (<code>double</code>)	<code>int</code> (<code>double</code>)
<code>ceil (x)</code>	<code><cmath></code>	Returns the smallest whole number that is not less than <code>x</code> : <code>ceil (56.34) = 57.0</code>	<code>double</code>	<code>double</code>
<code>cos (x)</code>	<code><cmath></code>	Returns the cosine of angle: <code>x</code> : <code>cos (0.0) = 1.0</code>	<code>double</code> (radians)	<code>double</code>
<code>exp (x)</code>	<code><cmath></code>	Returns e^x , where $e = 2.718$: <code>exp (1.0) = 2.71828</code>	<code>double</code>	<code>double</code>
<code>fabs (x)</code>	<code><cmath></code>	Returns the absolute value of its argument: <code>fabs (-5.67) = 5.67</code>	<code>double</code>	<code>double</code>
<code>floor (x)</code>	<code><cmath></code>	Returns the largest whole number that is not greater than <code>x</code> : <code>floor (45.67) = 45.00</code>	<code>double</code>	<code>double</code>
<code>islower (x)</code>	<code><cctype></code>	Returns <code>true</code> if <code>x</code> is a lowercase letter; otherwise, it returns <code>false</code> ; <code>islower ('h')</code> is <code>true</code>	<code>int</code>	<code>int</code>
<code>isupper (x)</code>	<code><cctype></code>	Returns <code>true</code> if <code>x</code> is an uppercase letter; otherwise, it returns <code>false</code> ; <code>isupper ('K')</code> is <code>true</code>	<code>int</code>	<code>int</code>
<code>pow (x, y)</code>	<code><cmath></code>	Returns x^y ; if <code>x</code> is negative, <code>y</code> must be a whole number: <code>pow (0.16, 0.5) = 0.4</code>	<code>double</code>	<code>double</code>
<code>sqrt (x)</code>	<code><cmath></code>	Returns the nonnegative square root of <code>x</code> ; <code>x</code> must be nonnegative: <code>sqrt (4.0) = 2.0</code>	<code>double</code>	<code>double</code>
<code>tolower (x)</code>	<code><cctype></code>	Returns the lowercase value of <code>x</code> if <code>x</code> is uppercase; otherwise, it returns <code>x</code>	<code>int</code>	<code>int</code>

EXAMPLE 1: The Square Root Function `sqrt ()`

```
#include <iostream>
#include <math.h>
// Test-driver for the sqrt function:
main0
{
for (int i = 0; i < 6; i++)
    Cout << "\t" << i << "\t" << sqrt(i) << endl;
}
```

Home work: by using predefined function prove the following

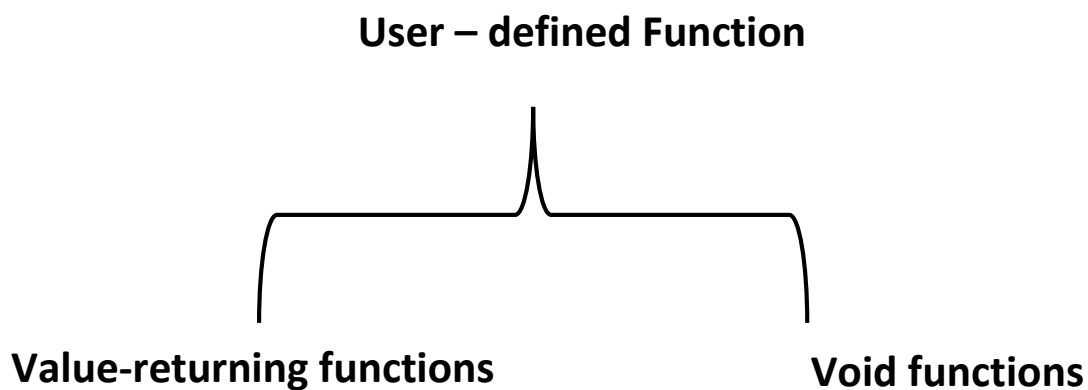
Trigonometry:

$$\sin 2x = 2 \sin x \cos x$$

try $x = 0$ to 2 incremented by 0.2

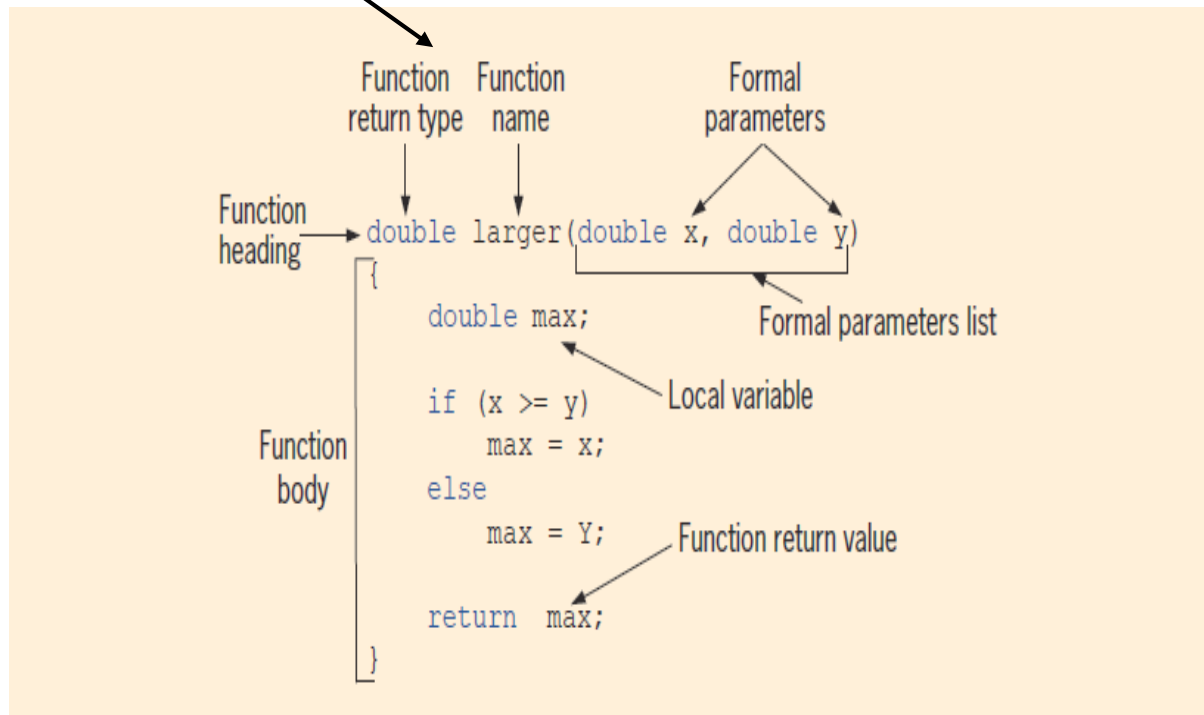
User-Defined Functions

Because C++ does not provide every function that you will ever need and designers cannot possibly know a user's specific needs, you must learn to write your own functions.

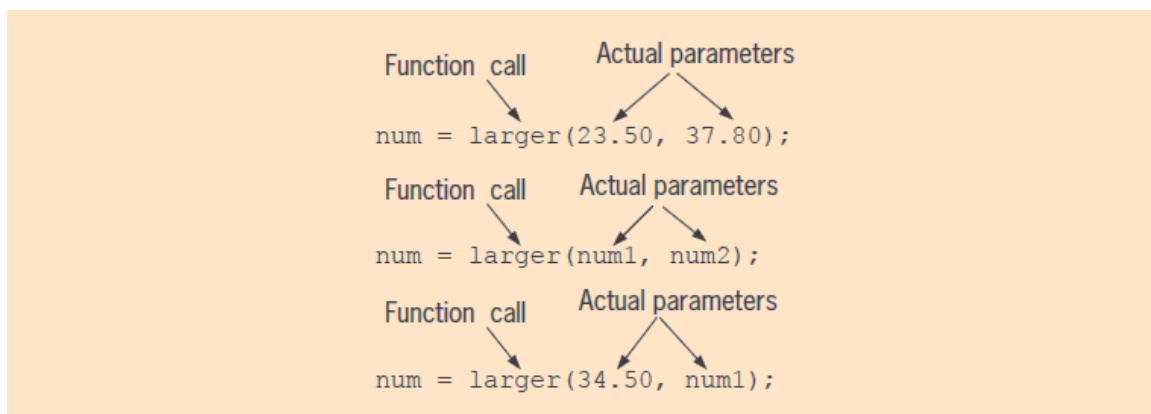


Terminology:

Inside function



Inside main



Example 2: cube () Function

Here is a simple example of a user-defined function:

// Returns the cube of the given integer:

```
int cube(int x)
{
    return x*x*x;
}
```

The function returns the cube of the integer passed to it. Thus cube (2) would return 8.

Here is a complete program, consisting of our `cube` function followed by a test driver:

// Returns the cube of the given integer:

```
int cube(int x)
{
    return x*x*x;
}
```

// Test driver for the cube function:

```
Main( )
{
    int n = 1;
    while (n != 0) {
        cin >> n;
        cout << cube(n) << endl;
    }
}
```

Example 3: The factorial () Function

The factorial of a positive integer n is the number $n!$ Obtained by multiplying n by all the positive integers less than n :

$$n! = (n) (n - 1) \dots (3) (2) (1)$$

For example, $5! = (5) (4) (3) (2) (1) = 120$.

Here is an implementation of the factorial function:

```
int factorial(int n)
{
    if (n < 0) return 0;
    int f = 1;
    while (n > 1)
        f *= n--;
    return f;
}
```

Example 4: The Permutation Function

A permutation is an arrangement of elements taken from a finite set. The permutation function $P(n,k)$ gives the number of different permutations of any k items taken from a set of n items. One way to compute this function is by the formula

$$p(n, k) = \frac{n!}{(n - k)!}$$

For example:

$$p(5, 2) = \frac{5!}{(5 - 2)!} = \frac{5!}{3!} = \frac{120}{6} = 20$$

// Returns $P(n,k)$, the number of permutations of k from n :

```
int perm(int n, int k)
{
    if (n < 0 || k < 0 || k > n) return 0;
    return factorial(n)/factorial(n-k);
}
```

Here is a test driver for the `perm ()` function:

```
int perm(int,int);

main ()
{
    for (int i = -1; i < 8; i++) {
        for (int j = -1; j <= i; j++)
            Cout << " " << perm(i,j);
        Cout << endl;
    }
}
```

References:

- [1] Deitel, P. & Deitel, R., "C++ How to Program", Eighth Edition, Pearson Education Inc., 2012.
- [2] Stefan B., " C++ Primer Plus ", Sixth Edition, Pearson Education Inc., 2012.